## X101/11/01

| NATIONAL | TUESDAY, 6 MAY |
| :--- | :--- |
| QUALIFICATIONS | 9.00 AM -9.45 AM |

MATHEMATICS<br>INTERMEDIATE 2<br>Units 1, 2 and<br>Applications of Mathematics<br>Paper 1<br>(Non-calculator)

## Read carefully

1 You may NOT use a calculator.
2 Full credit will be given only where the solution contains appropriate working.
3 Square-ruled paper is provided. If you make use of this, you should write your name on it clearly and put it inside your answer booklet.

## FORMULAE LIST

Sine rule: $\quad \frac{a}{\sin \mathrm{~A}}=\frac{b}{\sin \mathrm{~B}}=\frac{c}{\sin \mathrm{C}}$

Cosine rule: $\quad a^{2}=b^{2}+c^{2}-2 b c \cos \mathrm{~A}$ or $\cos \mathrm{A}=\frac{b^{2}+c^{2}-a^{2}}{2 b c}$

Area of a triangle: $\quad$ Area $=\frac{1}{2} a b \sin \mathrm{C}$

Volume of a sphere: $\quad$ Volume $=\frac{4}{3} \pi r^{3}$

Volume of a cone: $\quad$ Volume $=\frac{1}{3} \pi r^{2} h$

Volume of a cylinder: Volume $=\pi r^{2} h$

Standard deviation: $\quad s=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n-1}}=\sqrt{\frac{\sum x^{2}-\left(\sum x\right)^{2} / n}{n-1}}$, where $n$ is the sample size.

## ALL questions should be attempted.

1. 



Find the equation of the straight line shown in the diagram above.
2. Multiply out the brackets and collect like terms.

$$
(3 x+2)(x-5)+8 x
$$

3. A network diagram is shown below.

(a) Name an odd node.
(b) How many arcs are shown?
4. Woods Motors uses a spreadsheet to record the earnings for each employee.

An extract from their spreadsheet is shown below.

|  | A | B | C | D | E | F | G |
| :--- | :--- | :--- | ---: | ---: | ---: | ---: | :---: |
| 1 | Name | Basic <br> Salary | Commission <br> Jan-Mar | Commission <br> Apr-Jun | Commission <br> Jul-Sept | Commission <br> Oct-Dec | Total <br> Earnings |
| 2 | Ben | 12500 | 2000 | 2500 | 2750 | 1000 |  |
| 3 | Jasmine | 14000 | 1000 | 1000 | 1750 | 500 |  |
| 4 | Masha | 16750 | 1000 | 2000 | 2500 | 1250 |  |
| 5 | Umar | 18000 | 2500 | 1750 | 2750 | 2500 |  |

Which one of the following is a correct formula that could be used in cell G3 to calculate Jasmine's total earnings for the year?
$\mathrm{A}=\operatorname{SUM}(\mathrm{B} 3: \mathrm{F} 3)$
B $\quad \mathrm{SUM}=(\mathrm{B} 3: F 3)$
C $\quad \mathrm{G} 3=\operatorname{SUM}(\mathrm{B} 3: \mathrm{F} 3)$
5. At a ski resort the temperature, in degrees Celsius, was recorded each day at noon for the first fortnight in February 2013.

$$
\begin{array}{llllllllllllll}
0 & -1 & 2 & -5 & 4 & 2 & -3 & 1 & -4 & 8 & -6 & 4 & -2 & 1
\end{array}
$$

(a) Calculate:
(i) the median temperature; $\mathbf{1}$
(ii) the lower quartile; 1
(iii) the upper quartile. 1
(b) Use the above data to construct a boxplot.
(c) The temperature, in degrees Celsius, was recorded at the same ski resort each day at noon for the first fortnight in February 2014.

The following boxplot was constructed.


Compare the two boxplots and comment.
6. Below is a copy of Marta Ronaldo's credit card statement.

## Western Bank Finance

Name: Marta Ronaldo
Date: 18th May 2014

Account No 19502114
Credit limit: $£ 1500$
Interest rate: $2 \%$ per month

Please ensure your payment arrives by 30th May 2014

| 18 April 2014 | Balance brought forward | $370 \cdot 58$ |  |
| :--- | :--- | ---: | ---: |
| 24 April 2014 | Payment - Thank you |  | -50.00 |
|  | Interest (at 2\%) | 6.41 |  |
|  |  |  |  |
|  |  | $440 \cdot 00$ |  |
| 6 May 2014 | Mi Esposa Gowns | $52 \cdot 60$ |  |
| 10 May 2014 | Las Tapas Deliciosas | $35 \cdot 01$ |  |
| 12 May 2014 | Briggs Service Station | $\underline{ }$ |  |
| Balance owed |  | $854 \cdot 60$ |  |

Minimum payment: $5 \%$ of balance owed or $£ 20$, whichever is greater.
Note: Interest is charged each month on outstanding balance after payment is deducted.

Marta makes the minimum payment.
How much is the minimum payment?
7.


In triangle $\mathrm{PQR}, \mathrm{PQ}=5$ centimetres, $\mathrm{QR}=7$ centimetres and $\cos \mathrm{Q}=\frac{1}{5}$.
Calculate the length of side PR.
Give your answer in the form $\sqrt{a}$.
8. An ellipse has equation

$$
\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1
$$

Its area is given by the formula

$$
A=\pi a b .
$$

Find the area of an ellipse with equation

$$
\frac{x^{2}}{25}+\frac{y^{2}}{4}=1
$$

Take $\pi=3 \cdot 14$.
9. At a football match some spectators were asked how much money they spent at half-time.

The results of the survey are shown in the frequency table below.

| Money spent (£) | Frequency |
| :---: | :---: |
| $0 \leq p<2$ | 2 |
| $2 \leq p<4$ | 14 |
| $4 \leq p<6$ | 30 |
| $6 \leq p<8$ | 40 |
| $8 \leq p<10$ | 10 |

(a) Using squared paper, draw a histogram to illustrate the results of the survey.
(b) For the histogram you have drawn, estimate the mode.
10. The diagram below shows a circle, centre C .


The radius of the circle is 15 centimetres.
A is the mid-point of chord PQ .
The length of $A B$ is 27 centimetres.
Calculate the length of PQ .

## X101/11/02

NATIONAL TUESDAY, 6 MAY
QUALIFICATIONS 2014 10.05 AM - 11.35 AM

MATHEMATICS<br>INTERMEDIATE 2<br>Units 1, 2 and<br>Applications of Mathematics<br>Paper 2

## Read carefully

1 Calculators may be used in this paper.
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3 Square-ruled paper is provided. If you make use of this, you should write your name on it clearly and put it inside your answer booklet.

## FORMULAE LIST

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Standard deviation: $\quad s=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n-1}}=\sqrt{\frac{\sum x^{2}-(\Sigma x)^{2} / n}{n-1}}$, where $n$ is the sample size.

1. There are 964 pupils on the roll of Aberleven High School.

It is forecast that the roll will decrease by $15 \%$ per year.
What will be the expected roll after 3 years?
Give your answer to the nearest ten.
2. (a) A candle is in the shape of a cylinder with diameter 10 centimetres and height 15 centimetres.


Calculate the volume of the candle.
Give your answer correct to 3 significant figures.
(b) A second candle is in the shape of a cone with a circular base of diameter 14 centimetres and height $h$ centimetres.


It has the same volume as the first candle.
Calculate $h$.
3. Factorise fully

$$
3 x^{2}+9 x-12
$$

4. Mr Smith and Mrs Curran both shop at the same store.
(a) Mr Smith bought 3 loaves and 2 packets of butter. The total cost was $£ 4 \cdot 73$.

Let $x$ pounds be the cost of a loaf and $y$ pounds be the cost of a packet of butter.
Write down an equation in $x$ and $y$ which satisfies the above condition.
(b) Mrs Curran bought 5 loaves and 3 packets of butter. The total cost was $£ 7 \cdot 52$. Write down a second equation in $x$ and $y$ which satisfies this condition.
(c) Use the equations in parts $(a)$ and (b) to find the cost of a loaf and the cost of a packet of butter.
5. A runner has recorded her times, in seconds, for six different laps of the running track.

| 53 | 57 | 58 | 60 | 55 | 56 |
| :--- | :--- | :--- | :--- | :--- | :--- |

(a) Calculate:
(i) the mean;
(ii) the standard deviation;
of these lap times.

## Show clearly all your working.

(b) She changes her training routine hoping to improve her consistency. After this change, she records her times for another six laps.
The mean is 55 seconds and the standard deviation 3.2 seconds.
Has the new training routine improved her consistency?
Explain clearly your answer.
6. Gerry saves 2 pence, 5 pence and 10 pence coins in a jar.

He thinks the probability of picking a 5 pence coin at random from the jar is $\frac{25}{20}$. Why is he wrong?
7. A Building Society offers its customers a new Diamond Account.

The flowchart below shows how to calculate the interest when a certain amount of money ( $£ \mathrm{~A}$ ) is invested for 1 year in this account.


Use the flowchart to calculate the interest earned on an amount of $£ 65000$ invested in an Internet account for 1 year.
8. In a race, boats sail round three buoys represented by $\mathrm{A}, \mathrm{B}$ and C in the diagram below.


B is 8 kilometres from $A$ on a bearing of $060^{\circ}$.
C is 11 kilometres from B.
A is 13 kilometres from C.
(a) Calculate the size of angle ABC.
(b) Hence find the size of the shaded angle.
9. Thomas has borrowed $£ 5000$ from one of these banks to buy a car.

| Amount borrowed $=£ \mathbf{5 0 0 0}$ borrowed over 5 years |  |
| :---: | :---: |
| BANK | Monthly repayment |
| Regular Bank | $£ 109 \cdot 45$ |
| Central Bank | $£ 111.71$ |
| V.I.P. Bank | $£ 113.99$ |
| South-Western Bank | $£ 116 \cdot 29$ |

This loan will cost him $£ 1702 \cdot 60$ over 5 years. From which bank did Thomas receive the loan?
10. Joan Simmons sells cosmetics. She earns a Basic Pay plus Commission of $3 \%$ on all her sales.
Her payslip for a week in February is only partially complete.

| Name <br> J. Simmons | Employee No. $551$ | Tax Code 720L | Week Ending $15 / 02 / 2013$ |
| :---: | :---: | :---: | :---: |
| Basic Pay <br> £ $191 \cdot 50$ | Bonus $£ 0 \cdot 00$ | Commission | Gross Pay |
| Nat. Insurance $£ 27 \cdot 86$ | Income Tax $£ 64.59$ | Pension $£ 27 \cdot 53$ | Deductions |
|  |  |  | Net Pay $£ 352 \cdot 02$ |

Calculate Joan's sales for that week.
11. The table below illustrates the amount of money saved by 200 children over the past year.

| Money saved $(£)$ | Frequency |
| :---: | :---: |
| $0-9$ | 20 |
| $10-19$ | 40 |
| $20-29$ | 36 |
| $30-39$ | 44 |
| $40-49$ | 13 |
| $50-59$ | 22 |
| $60-69$ | 10 |
| $70-79$ | 15 |

Calculate the mean amount of money saved by the children.
12. The picture shows the entrance to a tunnel which is in the shape of part of a circle.


The diagram below represents the cross-section of the tunnel.


- The centre of the circle is O.
- MN is a chord of the circle.
- Angle MON is $50^{\circ}$.
- The radius of the circle is 7 metres.

Calculate the area of the cross-section of the tunnel.
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